## GED Knowledge & Skill Gaps Math—Session 1

A Tuesdays for Teachers Webinar by the GED Testing Service<sup>®</sup> October 26, 2021



#### Before We Get Started

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## **Today's Focus**

Some test takers and students have gaps in the knowledge and skills that they need to succeed on the GED Mathematical Reasoning test. Test takers and students may need more coverage and practice in these areas during test preparation.



#### What we will be covering

- How items and tests are developed
- How skill/knowledge gaps are identified
- Specific skills and GED indicators where students and test takers have the most difficulty
- Possible reasons why students and test takers are having difficulty





#### What we won't be covering

Test takers tend to perform less well on some items simply because the concepts they assess are more difficult.

In other words, we *expect* the items to be hard because the concepts are hard (e.g., permutations and quadratic equations).



#### Item development

Guiding principles for developing items include:

- > One item, one construct
- No extraneous numbers
- Distractors reflect (most) common mistakes
- > No trick questions
- > No testing of solution *methods*

All items are reviewed by outside experts (i.e., people like you) before they go on a test



#### Field test construction



Once an item is perfect\*, it is placed in a field test pool Field test items are embedded in operational—i.e., 'real'—tests Once enough test takers have taken the FT items, the pool is swapped out for another one

\*explained next slide



#### Post-test analysis

Field test items are analyzed statistically, *and* for content issues, then are designated as:

- accepted
- rejected
- revised/re-field tested

This statistical analysis is where knowledge and skill gaps are identified.





#### Areas of interest

#### Session 1:

- non-calculator items
- exponents/roots
- three-dimensional shapes

#### Session 2:

- algebraic computation
- inequalities
- slope/graphing
- multiple correct answers
- NOTE: there is overlap between some of these areas



#### Gap 1: Non-calculator items

On many non-calculator items, there is little difference in performance among high-, middle-, and low-achieving groups. This *may* be due to over-reliance on calculators during instruction and practice. GED<sup>®</sup> students should have practice on the skills assessed by the non-calculator indicators *without* the use of a calculator.



## Gap 1: Non-calculator items (indicators)

Non-calculator indicators:

- Q.1.a Q.1.d (number sense—ordering fractions/decimals, factors, multiples, exponents, distance on number lines)
- Q.2.a Q.2.d (arithmetic computation—four basic operations, order of operations, squares, cubes, roots, undefined expressions)
- > **NOT** Q.2.e (arithmetic word problems; calculator allowed)



#### Gap 1: Non-calculator items (examples)

Place 3/9, 4/11, and 3/7 in order from least to greatest. (Q.1.a)

What is the least common multiple of 3, 8, and 10? (Q.1.b)

Simplify  $(-2)^6 \times [(-2)^3]^2$ (Q.1.c)



Gap 1: Non-calculator items (examples)

Multiply 3/5 × 0.45 (Q.2.a)

Simplify  $-4 \times 5 + (36 \div 3) \div 2$ (Q.2.a)

Simplify  $-3\sqrt[3]{64}$ 



## Gap 2: Exponents/roots (indicators)

- $a^2$
- Specific indicators: Q.1.c (laws of exponents); Q.2.c (cubes/cube roots)
- Related indicators: Q.4, Q.5 (measurement of 2-D and 3-D shapes); Q.4.a (Pythagorean theorem); A.1.d – A.1.f & A.1.i (computing with, factoring, and evaluating polynomials); A.7.c – A.7.d (quadratic functions)
- Q.2.b (squares/square roots): test takers are mostly fine with this, but struggle a bit with squaring negatives





Simplify (-2)<sup>6</sup>(-2<sup>3</sup>)<sup>2</sup> (Q.1.c)

Simplify  $-3\sqrt[3]{64}$ (Q.2.c)

Simplify -6<sup>2</sup> (answer: -36) Simplify (-6)<sup>2</sup> (answer: 36) (explanation next slide) (Q.2.b)





PEMDAS (Please Excuse My Dear Aunt Sally) Parentheses, Exponents, Add/Subtract, Multiply/Divide

 $(-6)^2$  = squaring of -6 -6<sup>2</sup> = the negative of the square of 6 negative sign is equivalent to Subtract(ing) Exponents first; 6<sup>2</sup> = 36; negative of 36 = -36





A right triangle has two legs measuring 6 inches and 8 inches. What is the length, in inches, of the hypotenuse of the right triangle? (formula:  $a^2 + b^2 = c^2$ ) (Q.4.a)



What is the volume, in cubic inches, of a cone a radius of 3 inches and a height of 8 inches?

## Gap 2: Exponents/roots (examples)

What is the volume, in cubic inches, of a cylinder with a radius of 3 inches and a height of 8 inches?  $(V = \pi r^2 h)$ 

What is the volume, in cubic inches, of a cone with a radius of 3 inches and a height of 8 inches?  $(V = \frac{1}{3}\pi r^2 h)_{(Q.5.d)}$ 





Add  $(3x^2 - 4y^2) + (x^2 + 2y^2)$ (A.1.d)

What is the value of  $3x^2 - 4y^2$  when x = -3 and y = 2? (A.1.e)

Multiply 
$$(3x^3 - 4y^3)(x^3 + 2y^3)$$
  
(A.1.d)

Completely factor  $6x^8 - 12x^4 + 9x^2$ (A.1.f)



# Gap 3: Three-dimensional shapes (indicators)

Skills assessed (Q.5):

- calculate surface area
- calculate volume
  - determine dimensions (e.g., length, height, radius)

Figures: prisms, pyramids, cones, cylinders, spheres, composite figures

Formulas for surface area and volume of all figures assessed are provided on the GED Formula Sheet.



## Gap 3: Three-dimensional shapes (examples)

A sphere has a diameter of 12 inches. What is the surface area, in square inches, of the sphere?

```
(SA = 4\pi r^2)
(Q.5.d)
```

A cylinder has a radius of 2 inches and a height of 8 inches. What is the volume, in cubic inches, of the cylinder?

$$(V = \pi r^2 h)$$

(Q.5.b)



# Gap 3: Three-dimensional shapes (examples)

A sphere has a surface area of 200.96 square inches. What is the radius, in inches, of the sphere?

$$(SA = 4\pi r^2)$$

A cylinder has a volume of 401.92 cubic inches and a height of 8 inches. What is the radius, in inches, of the cylinder?

 $(V = \pi r^2 h)$ 

(Q.5.b)





#### Resources on GED.com

- Computer Tutorial
- Calculator Tutorial
- Calculator Reference Sheet
- Formula Sheet
- Math Study Guide
- Calculator-Prohibited Indicators





#### **Computer Tutorial**





#### Calculator

#### https://ged.com/wpcontent/uploads/calculator\_sheet.pdf



https://ged.com/practice-test/en/calculator/

Available in English and Spanish

HMETIC

ASIC

AGES

NOTATION

CIENTIFIC

FRACTIONS

EXAMPLE RH

8

EXAMPLE PERCENT

4

EXAMPLE

7



#### Formulas

https://ged.com/wpcontent/uploads/math\_formula\_ sheet.pdf

#### Available in English and Spanish

2014 GED<sup>®</sup> Test Resources



#### **Mathematics Formula Sheet & Explanation**

The 2014 GED® Mathematical Reasoning test contains a formula sheet, which displays formulas relating to geometric measurement and certain algebra concepts. Formulas are provided to test-takers so that they may focus on *application*, rather than the *memorization*, of formulas.

Area of a:			
square	$A = s^2$		
rectangle	A = hv		
parallelogram	A = bh $A = \frac{1}{2}bh$		
triangle			
trapezoid	$A = \frac{1}{2}h(b_1 + b_2)$		
dirde	$A = \pi r^2$		
Perimeter of a:			
square	P = 4s		
rectangle	P = 2/+ 2w		
tiangle	$P = s_1 + s_2 + s_3$ $C = 2\pi r \text{ OR } C = \pi d$ ; $\pi = 3.14$		
Circumference of a circle			
Surface area and volume of a:			
rectangular prism	SA = 2hw + 2hh + 2wh	V = hwh	
right prism	SA = ph + 2B	V = Bh	
cylinder	$SA = 2\pi r h + 2\pi r^2$	$V = \pi r^2 h$	
pyramid	$SA = \frac{1}{2}ps + B$	$V = \frac{1}{3}Bh$	
cone	$SA = \pi rs + \pi r^2$	$V = \frac{1}{2}\pi r^2 h$	
sphere	SA = 4π/ <sup>2</sup>	$V = \frac{4}{7} m^2$	
	(p = perimeter of base with are	ea B: π = 3.14)	
Data			
Data mean	mean is equal to the total of the the number of elements in the	e values of a data set, divided by data set	
Data mean median	mean is equal to the total of th the number of elements in the median is the middle value in a of a data set, or the mean of th number of ordered values in a	e values of a data set, divided by data set an odd number of ordered values the two middle values in an even data set	
Data mean median Algebra	mean is equal to the total of th the number of elements in the median is the middle value in a of a data set, or the mean of th number of ordered values in a	the values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	
Data mean median Algebra slope of a line	mean is equal to the sotal of the the number of elements in the median is the middle value in a of a data set, or the mean of the number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$	e values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	
Data mean median Algebra slope of a line slope-intercept form of the equation of a line	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of the number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$ $y = mx + b$	e values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	
Data mean median Algebra slope of a line slope-intercept form of the equation of a line point-slope form of the equation of a line	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of it number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$ $y = mx + b$ $y - y_1 = m(x - x_1)$	te values of a data set, divided by data set an odd number of ordered values ne two middle values in an even data set	
Data mean median Algebra slope of a line slope-intercept form of the equation of a line point-slope form of the equation of a line standard form of a quadratic equation	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of it number of ordered values in a $m = \frac{y_2 - y_2}{x_2 - x_1}$ $y = mx + b$ $y - y_1 = m(x - x_1)$ $y = ax^2 + bx + c$	te values of a data set, divided by data set an odd number of ordered values ne two middle values in an even data set	
Data mean median Algebra slope of a line slope-intercept form of the equation of a line point-slope form of the equation of a line standard form of a quadratic equation quadratic formula	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of th number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$ $y = mx + b$ $y - y_1 = m(x - x_1)$ $y = ax^2 + bx + c$ $x = \frac{-b \pm \sqrt{b^2 - 4ax}}{a}$	e values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	
Data mean median Algebra slope of a line slope-intercept form of the equation of a line point-slope form of the equation of a line standard form of a quadratic equation quadratic formula Pythagorean theorem	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of the number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$ $y = mx + b$ $y - y_1 = m(x - x_1)$ $y = ax^2 + bx + c$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $a^2 + b^2 = c^2$	e values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	
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Data mean median Algebra slope of a line slope-intercept form of the equation of a line point-slope form of the equation of a line standard form of a quadratic equation quadratic formula Pythagorean theorem simple interest	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of the number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$ $y = mx + b$ $y - y_1 = m(x - x_1)$ $y = ax^2 + bx + c$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $a^2 + b^2 = c^2$ $l = Prt$ $(l = interest, P = principal, r = r$	ne values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	
Data mean median Algebra slope of a line slope-intercept form of the equation of a line point-slope form of the equation of a line standard form of a quadratic equation quadratic formula Pythagorean theorem simple interest distance formula	mean is equal to the total of the the number of elements in the median is the middle value in a of a data set, or the mean of the number of ordered values in a $m = \frac{y_2 - y_1}{x_2 - x_1}$ $y = mx + b$ $y - y_1 = m(x - x_1)$ $y = ax^2 + bx + c$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $a^2 + b^2 = c^2$ $I = Prt$ $(I = interest, P = principal, r = r)$ $d = rt$	re values of a data set, divided by data set an odd number of ordered values he two middle values in an even data set	

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#### Math Study Guide

-	1/24/2018 MyGED® : Study Guide
	3 Simplify exponents
1/24/2018 MvGFD® - Study Guide	Simplify numerical expressions with exponents
GED Study Guide	For example, $2^6 \times 2^5 = 2^{11}$
х+уз матн	Example Questions
What you need to know about the GED <sup>®</sup> Math Test	Simplify exponents
You should be familiar with arithmetic and math concepts, measurements, equations, and applying math concepts to solve real-life problems. Remember the math test is not a memorization test? You'll have access to a formula sheet that gives you information like how to calculate the area for	Question:
onevent shapes. 2 This study guide and the example questions in it will help you get an idea of what's going to be on the test.	$(2^9 imes 3^6) imes (2^4 imes 3)^2$
You <u>don't</u> need to know everything in this guide!	(A) 6 <sup>20</sup>
If you want to see how close you are to passing, the GED Ready <sup>®</sup> official practice test is a great way to help you determine if you're ready.	(B) 6 <sup>24</sup>
Test Overview	© 2 <sup>13</sup> × 3 <sup>7</sup>
Topics Rational Numbers Shapes and Measurement	<b>D</b> $2^{17} \times 3^7$
Graphs and Functions Expressions and Equations	
Time (to take the test) 1/24/2018 MyGED	08 : Study Guide
3 minute break between parts (to retrieve your calculator) Basic Math	
Calculator wed for part 2 A calculator references the and math formula sheet	
Multiple choice and other question types (drag and drop, fill in the bi	
What you'll be tested on Place fractions and decimals in order.	
The GED test will measure your strength in the skills below. Click on a skill to le 1 0.5 3 0.9	
4 <sup>1000</sup> 8 <sup>1000</sup> in order from smallest to largest	
$\frac{1}{7}, \frac{3}{7}, 0.5, 0.9$	
Fyamle Questions	
Example Quotions	
Fractions and decimals in order	
Question: Between which pair of decimals should $\frac{4}{7}$ be placed on a number lim	ie?
(À) 0.3 and 0.4	
(B) 0.4 and 0.5	
© 0.5 and 0.6	
(D) 0.6 and 0.7	
	https://ged.com/wp-content/upload
28	Guide Math pdf

#### **Calculator Prohibited Indicators**



#### TEST-TAKER RECOMMENDATIONS FOR CALCULATOR-PROHIBITED INDICATORS

The first several questions of the GED<sup>®</sup> Mathematical Reasoning test assess eight indicators covering various concepts in number sense and computation (Q.1.a through Q.1.d and Q.2.a through Q.2.d) that prohibit the use of the calculator. GED Testing Service has analyzed data on these calculator-prohibited items, resulting in the following comments and recommendations:

Indicator	Background	Recommendations for Test-takers
<b>Q.1.a</b> Order fractions and decimals, including on a number line.	<ul> <li>These questions may require</li> <li>comparing or ordering positive numbers, or negative numbers, or both,</li> <li>with or without a number line.</li> <li>Test takers generally do very well on this indicator, with the exception of questions that require test takers to compare or order a set consisting entirely of <i>negative</i> numbers.</li> </ul>	<ul> <li>Leverage skills in comparing and ordering <i>positive</i> fractions and decimals toward similar skills comparing and ordering <i>negative</i> fractions and decimals.</li> <li>Understand the difference in how negative numbers are compared and ordered:         <ul> <li>For instance, while 0.7 is greater than 0.2, -0.7 is actually <i>less than</i> -0.2.</li> <li>Since positives and negatives are essentially opposites, the rules for ordering each type of number are applied in a similarly opposite manner.</li> </ul> </li> </ul>
<b>Q.1.b</b> Apply number properties involving multiples and factors, such as using the least common multiple, greatest common factor, or distributive property to rewrite numeric expressions.	Test takers generally perform very well on this indicator, which includes questions that include both context or pure computation (no context) and which test factors of a number, multiples of a number, least common multiple, greatest common factor, etc.	No specific recommendations are provided, as the general population of GED <sup>®</sup> test takers performs well on this indicator.



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#### **Instructional Resources**

- Florida Literacy Math App
- Effortless Math
- IXL Learning
- GED Math Crash Course
- Math is Fun





#### Florida Literacy Math App



Scan with camera to access app

https://floridaliteracy.org/mathvideos.html

#### 3:49 1 ≡ Welcome



#### VIDEO MATH PREP FOR THE GED

This app is proudly presented to you by the Florida Literacy Coalition, in partnership with CrowdED Learning.

#### How to use this app

Watch this video to learn how to make the most of the app's features as you build your math skills!





#### Video Math Prep–GED

*by* CrowdED Learning and Florida Literacy Coalition

Built in collaboration by the Florida Literacy Coalition + CrowdED Learning

SHARE APP SHOW FULLSCREEN



#### FL Literacy Math App Tracking Sheet



Florida Literacy Coalition, Inc. FLC Math Tracking Sheet

This tracking sheet may help you as you explore all the video mini-lessons for the GED Math test. You can download/print this form and check the boxes next to the videos that you've watched.

It may be best if you watch the videos in order as they have been arranged with increasing difficulty and the skills will build as you go along.

As you explore the website you will notice that the videos are organized into 6 sections:

Foundations Basic Math Basic Algebra Graphs and Functions Geometry Calculator/Reference Sheet

These sections are shown below. When you open each section you will find the videos organized into subsections shown here in blue.

<u>Limited on time</u>? If you're looking for the most important videos you may want to focus on the <u>Basic Algebra</u> and <u>Graphs and</u> Functions sections.

#### FOUNDATIONS

# Place Value and Rounding Place Value and Rounding Finding a number's place value Rounding whole numbers example 1 Rounding whole numbers example 2 Rounding to estimate difference Rounding decimals to the nearest tenth Fraction Basics Numerator and denominator of a fraction Identifying fraction parts Proper and improper fractions Converting mixed numbers to improper fractions Mined numbers phaseing from an example

Mixed numbers: changing from an improper fraction

Fractions in lowest terms

Reciprocal of a mixed number

Finding Common denominators

Decimal Basics
Decimal place value

Decimal to simplified fraction
Fraction to decimal
Converting percent to decimal and
fraction

Identification

#### https://gedmath.glideapp.io/

	Recognizing prime and composite numbers	
	Identifying Rational Numbers	
	Identifying parallel and perpendicular lines	
	Properties and Laws	
	Properties of whole numbers	
	Commutative property for addition	
	Commutative law of addition	
	Associative law of addition	
	Associative property for multiplication	
	Associative law of multiplication	
	Commutative law of multiplication	
	Ways to represent multiplication	
	Identity Property	
	Distributive Property 3	
	Distributive law of multiplication	
	Expressing division in multiple ways	
BASIC MATH		
	Comparing Numbers	
	Comparing whole numbers, place value	
	Comparing decimals	
	Comparing fractions	
	Comparing fractions with different	



#### **Effortless Math**

This site contains free pdf worksheets for <u>TABE</u> and <u>GED</u> skills practice.

All worksheets contain answer keys so that students can self-check their work.



Download FREE printable PDF worksheets for the Mathematics portion of the TABE test.



Looking for free printable GED Math worksheets and exercises to help you prepare for the GED Mathematical Reasoning test?



## IXL Learning

Contains content for math (K-12), RLA (K-12), science (K-8), and social studies (K-8)





## **GED Math Crash Course**

This site contains videos, notes, and practice problems for GED(R) prep students

Website can be found here

Resources can be incorporated into a Google Classroom



Want to boost your math score in a hurry? Are you just a few points from passing your GED math test? Focusing on one of these GED Math favorite subjects is just what you need for a quick score boost.





#### Math is Fun

#### https://www.mathsisfun.com/geometry/



Geometry is all about shapes and their properties.

If you like playing with objects, or like drawing, then geometry is for you!

Geometry can be divided into:



Plane Geometry is about flat shapes like lines, circles and triangles ... shapes that can be drawn on a piece of paper



**Solid Geometry** is about three dimensional objects like cubes, prisms, cylinders and spheres.

Hint: Try drawing some of the shapes and angles as you learn ... it helps.

#### Point, Line, Plane and Solid

- A Point has no dimensions , only position
- A Line is one-dimensional
- A Plane is two dimensional (2D)
- A Solid is three-dimensional (3D)



#### Using Nets to Find Surface Areas

#### **Math Interactives**



http://www.learnalberta.ca/content/mejhm/index.html?l=0&ID1=AB.MATH.JR.SH AP&ID2=AB.MATH.JR.SHAP.SURF&lesson=html/object\_interactives/surfaceAre a/use\_it.html



Tuesdays for Teachers (coming this fall)

## Trends in Students' Knowledge & Skill Gaps

Co-presenters: GEDTS Content Area Specialists Test Development Division



## Tuesdays for Teachers 12:30-2:00 PDT/3:30-5:00 EDT

November 16, 2021	Mathematical Reasoning, Part Two
December 7, 2021	Reasoning Through Language Arts, Part One
January 25, 2022	Reasoning Through Language Arts, Part Two
February—March	<ul><li>Social Studies</li><li>Science</li></ul>
May 2022	<ul> <li>Individual "Hot Topic Sessions" based upon Educator and Administrator interest and GEDTS observations of student and educator trends</li> </ul>





## SUCCESS







# Thank you!

Communicate with GED Testing Service<sup>®</sup> help@ged.com

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