



Session Objectives

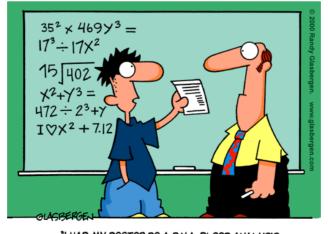


- Discuss the challenges students have with key concepts in math
- Focus on the foundational "must haves" in mathematical reasoning
- Review tips and strategies for helping students build consistency in math
- Share resources

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It Really Isn't Genetic



"I HAD MY DOCTOR DO A D.N.A. BLOOD ANALYSIS. AS I SUSPECTED, I'M MISSING THE MATH GENE."

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Math involves... • Memory • Language • Sequencing • Spatial ordering • Critical thinking • Good problem-solving strategies • Number sense • Reasoning • Making connections

In the Classroom, We Often...

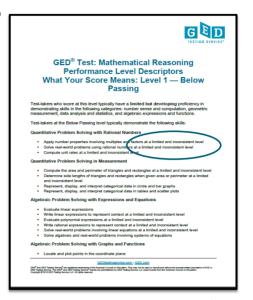
- Make assumptions about the presence or absence of foundational skills
- Introduce new concepts too rapidly
- Insufficiently support explanations and activities
- Provide insufficient practice
- Focus on facts versus concepts
- Limit access to manipulatives
- Limit connection of skills to real-life situations



What's the Problem?

Students at Level 1

- Have limited, but developing proficiency
- Perform some math skills at a basic level, such as
 - Putting fractions/decimals on a number line
 - Solving two-step arithmetic problems
- Are inconsistent in the application of skills
- Lack fluency in basic operations and mathematical properties





Performance Level Descriptors (PLDs)

- Helpful tool for the classroom
- Explain in detail the skills students need to demonstrate to pass the test





How to Use PLDs in the Classroom

Use PLDs to:

Tip 1: Assess student's current skill level

Tip 2: Determine when students are ready

to test

Tip 3: Shape learning activities

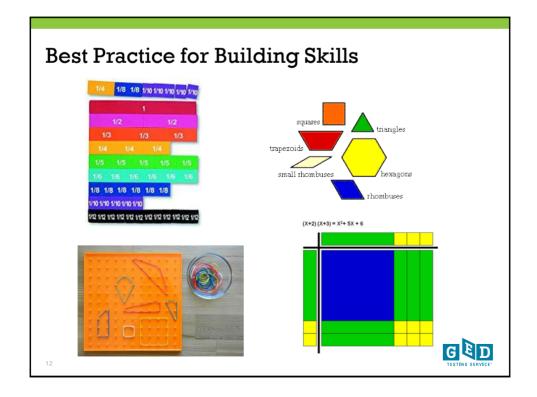
Tip 4: Add perspective to lesson plans



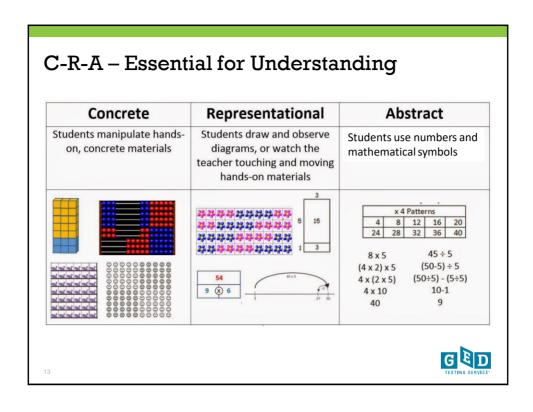
Our Students Need... A Balanced Mathematics Program WHERE Problem A Procedural MATHEMATICS Solving MATHEMATICS WORKS WORKS WORKS Perchanal Mail D Conceptual MATHEMATICS WORKS Perchanal Mail D CONSISTENCY CONSISTENCY CONSISTENCY CONSISTENCY CONSISTENCY

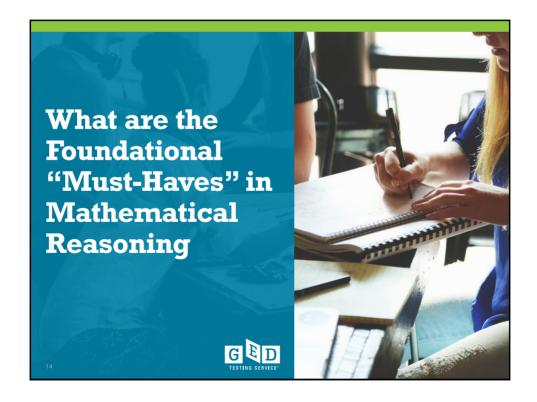
Math Grab Bag

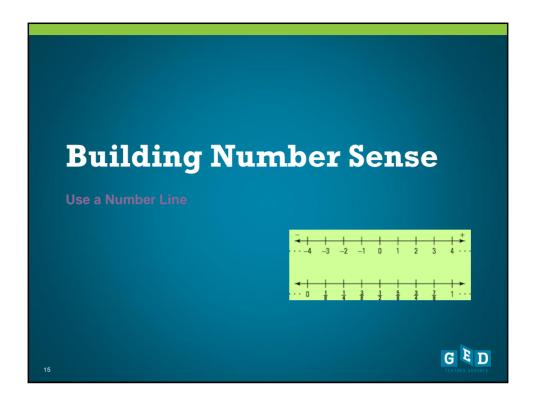
Low Intermediate Basic	High Intermediate	Low Adult Secondary
Education	Basic Education	Education
(4-5.9 GLE)	(6-8.9 GLE)	(9-10.9 GLE)
Students can perform with high accuracy all four basic math operations using whole numbers up to three digits and can identify and use all basic mathematical symbols.	Students can perform all four basic math operations with whole numbers and fractions; can determine correct math operations for solving narrative math problems and can convert fractions to decimals and decimals to fractions; and can perform basic operations on fractions.	Students can perform all basic math functions with whole numbers, decimals, and fractions; can interpret and solve simple algebraic equations, tables, and graphs and can develop own tables and graphs; and can use math in business transactions.



7/2018







Students with Number Sense...

- Think and reason flexibly with numbers
- Use numbers to solve problems
- Spot unreasonable answers
- Understand how to put numbers together and take them apart
- Understand number relationships

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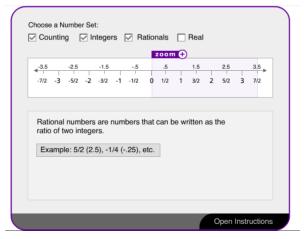
But they are just numbers...

Type of Number	Quick Description
Counting Numbers	{1, 2, 3,}
Whole Numbers	{0, 1, 2, 3,}
Integers	{, -3, -2, -1, 0, 1, 2, 3,}
Rational Numbers	p/q – p and q are integers, q is not zero
Irrational Numbers	π – 3.14159265358979323856 cannot be written as a simple fraction $\sqrt{3}$, $\sqrt{99}$
Real Numbers	Rational and Irrational

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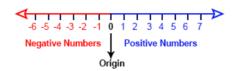
Defining Numbers



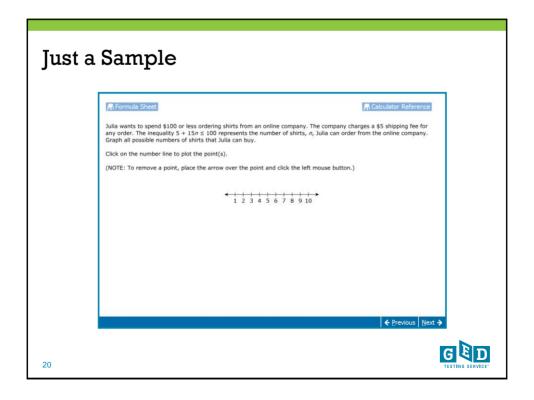
https://unctv.pbslearningmedia.org/resource/mgbh.math.ns.numbline/building-a-number-line/#.WU1B-IWcHnM

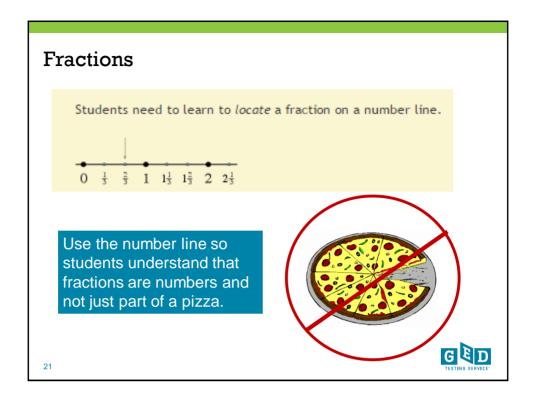
The Number Line

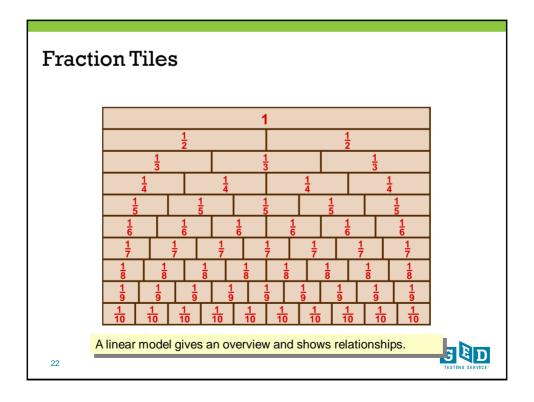
- Provides a model for basic operations for all rational numbers
- Is a spatial object
- Allows students to situate themselves spatially in mathematics
- Permits students to conceptualize mathematics



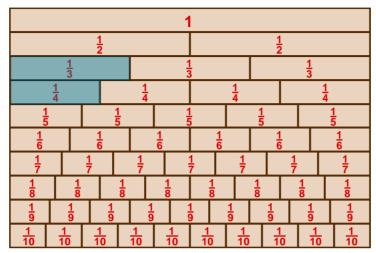
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Fraction Tiles



What is more, 1/4 or 1/3? What is more, 1/9 or 1/10?



Can students identify the problem?

(a)
$$\frac{2}{5} + \frac{1}{3} = \frac{3}{8}$$

b)
$$\frac{2}{7} + \frac{1}{3} = \frac{2}{21} + \frac{1}{21} = \frac{3}{21}$$

c)
$$\frac{3}{8} + \frac{1}{4} = \frac{9}{32} + \frac{8}{32} = \frac{17}{32}$$

d)
$$\frac{8}{9} + \frac{1}{4} = \frac{32}{36} + \frac{9}{36} = \frac{41}{72}$$

e)
$$\frac{7}{12} + \frac{5}{6} = \frac{14}{24} + \frac{20}{24} = \frac{34}{24} = \frac{17}{12}$$

f)
$$6\frac{1}{2} - 4\frac{2}{3} = 6 - 4 + \frac{1}{2} - \frac{2}{3} = 2 + \frac{3}{6} - \frac{4}{6} = 2\frac{1}{6}$$

b)
$$\frac{2}{7} + \frac{1}{3} = \frac{2}{21} + \frac{1}{21} = \frac{3}{21}$$
 g) $5\frac{2}{5} + 1\frac{3}{4} = 5\frac{8}{20} + 1\frac{15}{20} = 6\frac{23}{20} = 7\frac{3}{20}$

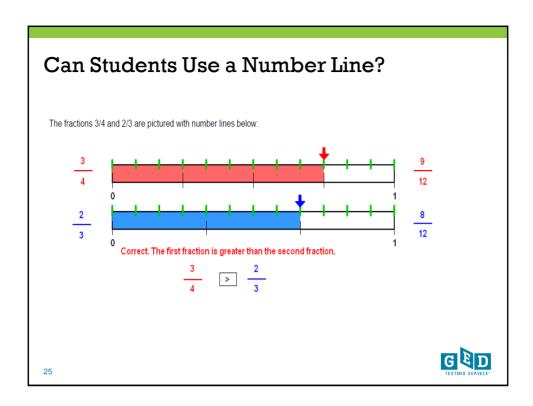
c)
$$\frac{3}{8} + \frac{1}{4} = \frac{9}{32} + \frac{8}{32} = \frac{17}{32}$$
 h) $\frac{1}{2} \times \frac{1}{5} = \frac{5}{10} \times \frac{2}{10} = \frac{10}{100} = \frac{1}{10}$

i)
$$2\frac{1}{2} \div 1\frac{3}{4} = \frac{5}{2} \times \frac{7}{4} = \frac{35}{8} = 4\frac{3}{8}$$

j)
$$\frac{17}{20} - \frac{4}{5} \times \frac{3}{8} = \frac{17}{20} - \frac{16}{20} \times \frac{3}{8} = \frac{1}{20} \times \frac{3}{8} = \frac{4}{160} = \frac{1}{40}$$

"Five out of four people have trouble with fractions."

-- Steven Wright



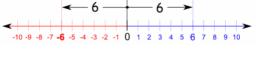
Absolute Value

Absolute Value means how far a number is from 0.

- Remove any negative sign and think of all numbers as positive
- Recognize symbol used to represent absolute value

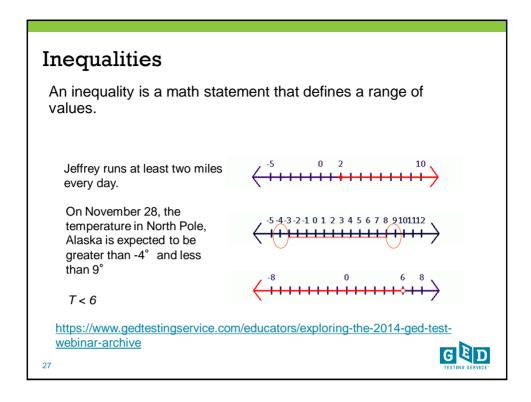
$$|-5| = 5$$

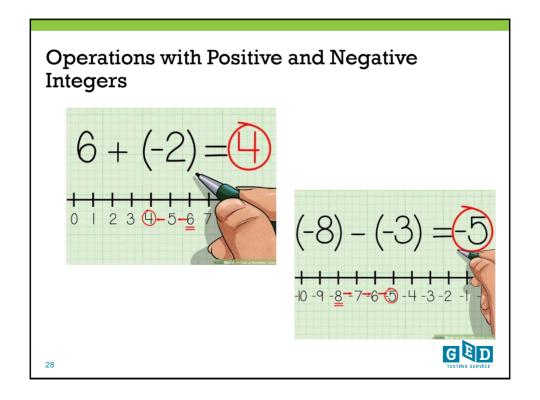
$$|7| = 7$$

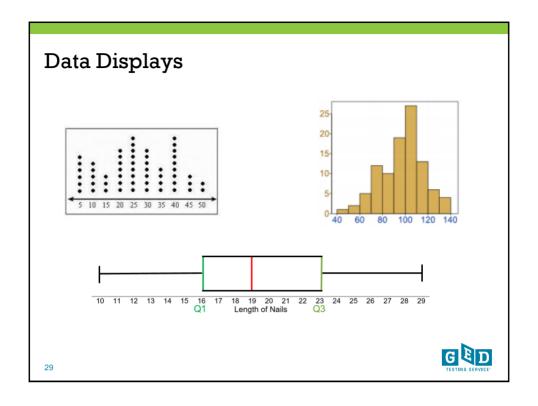


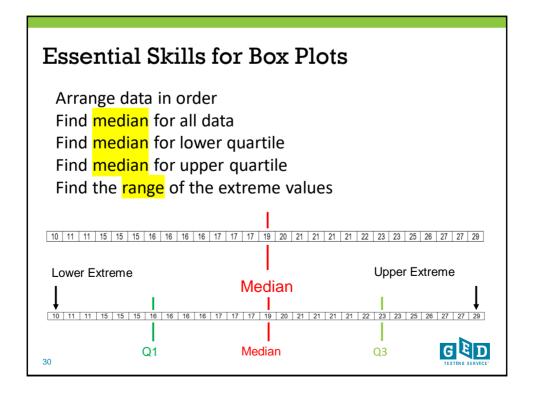
"6" is 6 away from zero, and "-6" is **also** 6 away from zero.

So the absolute value of 6 is 6, and the absolute value of -6 is also 6









Number Lines and the NFL



https://unctv.pbslearningmedia.org/resource/mket-math-ns-ratnumb/football/#.WU0tDGgrKUk

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Resources

Helping with Math - Number Line Generator

http://www.helpingwithmath.com/printables/others/NumberLineGenerator01.htm

Math Warehouse – Number Line Graph Maker

http://www.mathwarehouse.com/number-lines/number-line-maker.php

Math is Fun - Number Lines (Inequalities, Operations, etc.)

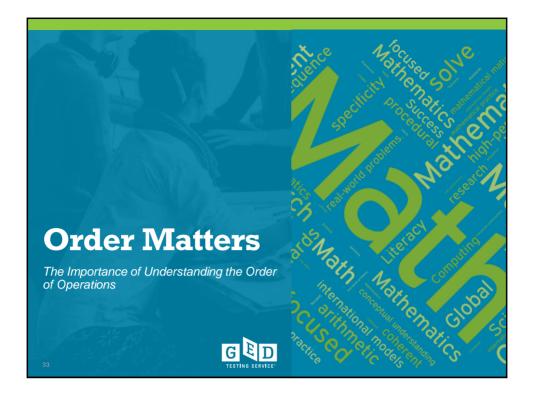
http://www.mathsisfun.com/numberline.html

Annenberg Learner – Building the Number Line

http://www.learner.org/courses/learningmath/number/session1/part_c/index.html





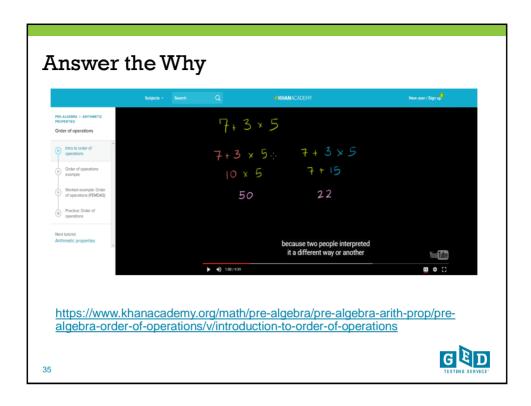


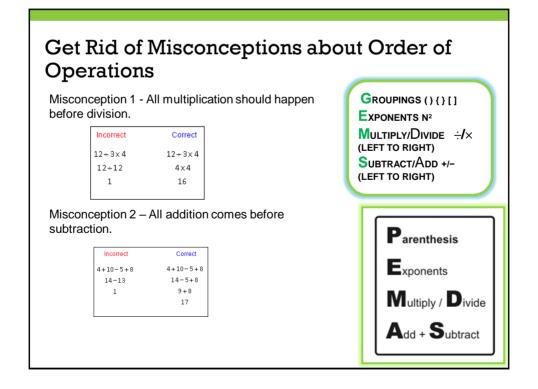
Why Bother?

Here is your problem: $4 + 2 \times 3 =$ Is the answer 18 or 10?

- Avoid confusion in how problems are solved
- Set up rules of precedence or rank of operations
- Is critical to simplifying and solving different algebra problems







Essential Understanding

- 1. Parentheses and Brackets from the inside out
- 2. Exponents of numbers or parentheses
- 3. Multiplication and Division in the order they appear
- 4. Addition and Subtraction in the order they appear





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Your Turn

What is the value of $6 \div 3 + 4 \times 2$?

So we do the division and multiplication before any addition or subtraction:

$$6 \div 3 + 4 \times 2$$

= 2 + 4 \times 2
= 2 + 8
= 10

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Your Turn

What is the value of $6 \times 4 - 12 \div 3 - 8$?

We do 6 \times 4 and 12 \div 3 first, then the subtractions:

$$6 \times 4 - 12 \div 3 - 8$$

= 24 - 12 \div 3 - 8
= 24 - 4 - 8
= 20 - 8
= 12



Your Turn

What is the value of 20 - $(3 \times 2^3 - 5)$?

We start inside the **P**arentheses, and then use "Exponents" first:

$$20 - (3 \times 2^3 - 5) = 20 - (3 \times 8 - 5)$$

[Because 2^3 means $2 \times 2 \times 2 = 8$, **not** $2 \times 3 = 6$]

Next **M**ultiply:

$$20 - (3 \times 8 - 5) = 20 - (24 - 5)$$

Next Subtract (still working inside the parentheses):

20 - (24 - 5) = 20 - 19

Now the Parentheses are completed, the last operation is **S**ubtract:

Your Turn

What is the value of $(12 \div 3 + 4) - (4^2 - 6 \times 2)$?

$$(12/3+4)-(4^2-6\times2)$$

$$= (4+4)-(4^2-6\times2)$$

$$= 8-(4^2-6\times2)$$

$$= 8-(16-6\times2)$$

$$= 8-(16-12)$$

$$= 8-4$$

$$= 4$$

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What's Your Sign?

In the equation below, replace each question mark with one of the four mathematical signs: $+,-,\times$, or \div . Each sign can be used only once. Fill in the blanks to solve the equation. (Hint: the first sign is +.)

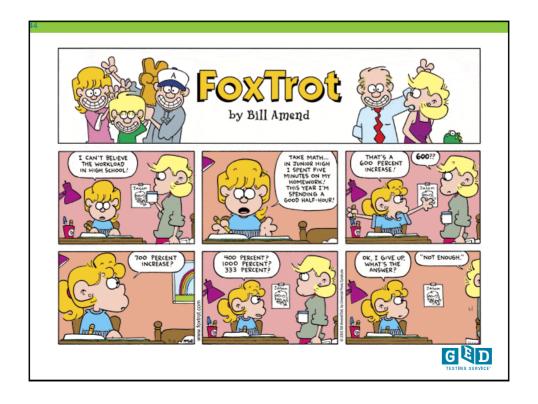
$$7?5?4?7?6=15$$

What is the first step that you need to take in order to solve the equation? Write your answer in the question box.

$$(7+5) \div 4 \times 7 - 6 = 15$$







Do your students know the vocabulary?

Ratio – a comparison between two different values Percent of change – ratio of the amount of change to the original amount

Percent increase – how much original amount increases Percent decrease – how much original amount decreases



percent change =

amount of change original amount



What do students need to know?

- An understanding of percent
- Part and whole
- Increase
- Decrease
- Original number
- Difference between percentage of and percent of change



Do they understand increase vs. decrease?

- If you buy a brand new car for \$15,999, drive it off the lot, and get into an accident, the car will be worth \$11,499. Does the car's value increase or decrease?
- The temperature at sunrise is 71 degrees Fahrenheit. At noon, the temperature is 84 degrees Fahrenheit. At sunset, it is 69 degrees Fahrenheit. Has the temperature had an increase or decrease from sunrise to sunset?
- A scuba diver jumps off a dive boat into the water and descends 30 feet below sea level. He rises 10 feet to swim above a coral head, then swims back down 8 feet to the top of a submerged wreck. Has his depth shown an increase or decrease from his initial descent?

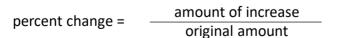
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Percent of Increase

- Tips
- Sales Tax
- Increase in Population

To calculate percent of increase





Calculating a Percent of Increase

In 1981, there were 25 endangered and threatened species of reptiles in the U. S. In 2015, there were 45 species. By what percent did the number of these reptile species change from 1981 to 2016?



Is the amount of change an increase or a decrease? (increase)

What is the amount of change from 1981 to 2015? (45 - 25 = 20)

What is the original amount? (25)

Divide the amount of change by the original amount (20/25 = .8)

Write the quotient as a percent (.8 = 80% increase)



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Calculating a Percent of Increase

198,000 people attended a concert in 2007. The number of attendees increase by 12% from 2007 to 2017. How many attendees attended in 2017?



- $= 198,000 + 198,000 \times 12\% \times (Substitute)$
- $= 198,000 + 198,000 \times 0.12$ (write percent as a decimal)
- =198,000 +
- = 221,760 (Evaluate)



Percent of Decrease

- Discounts
- Sales
- Reduction in Population



To calculate percent of decrease

percent change = amount of decrease original amount

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Calculating a Percent of Decrease

A stock was worth \$18.00 a share in 2000. In 2016, the same stock was worth \$7.60 a share. What was the percent of change?



Is the amount of change an increase or a decrease? (decrease)

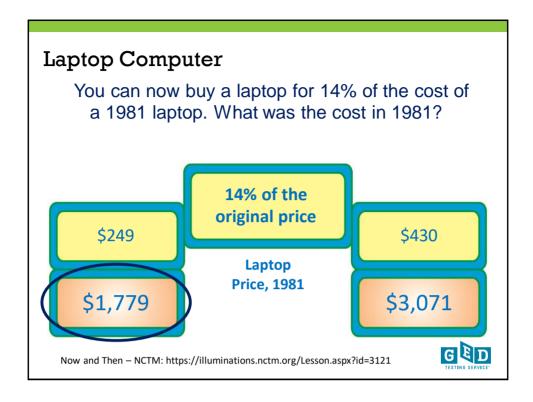
What is the amount of change from 2000 to 2016? (\$10.40)

What is the original amount? (\$18.00)

Divide the amount of change by the original amount (10.40/18)

Write the quotient as a percent (.57777 . . . = 58% decrease)

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Common Errors

- Using the wrong base when calculating change
- Not being able to differentiate between a quantity change and a percentage change
- Incorrectly changing a decimal to a percent
- Confusing "percentage of" situations with percent increase/decrease situations
- Not reading the situation (word problem) carefully

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Resources

Art of Problem Solving: Percent Increase and Decrease Part 1

https://www.youtube.com/watch?v=vTPQV_M6tfl

Art of Problem Solving: Percent Increase and Decrease Part 2

https://www.youtube.com/watch?v
=TbUlfWJ9Ohw

How to Find the Percent Change

Increase: The Easy Way
https://www.youtube.com/watch?v
=YWOeN7hDD3E

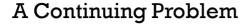
How To Find Percent Change Decrease: The Easy Way

https://www.youtube.com/watch?v =fwhZ8ITiReY

PERCENTS







Students think an exponent is the same as multiplication.



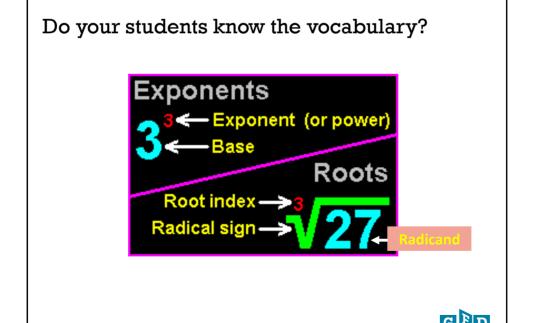
Multiplication = Repeated Addition

6 x 3 = 18 6 + 6 + 6 = 18

Exponents = Repeated Multiplication

 $6^3 = 18$ $6 \times 6 \times 6 = 216$







Rul	Rules of Exponents				
	Rule	Example			
1	x ¹ = x	51 = 5			
2	x ⁰ = 1	5 ⁰ = 1			
3	$x^{-1} = \frac{1}{x^1}$	$5^{-1} = \frac{1}{5}$			
4	$(x^m)(x^n) = x^{m+n}$	$(x^2)(x^3) = x^{2+3} = x^5$			
5	$\frac{x^m}{x^n} = x^{m-n}$	$\frac{x^3}{x^2} = x^{3-2} = x^1$			
6	$(x^m)^n = x^{(m)(n)}$	$(x^3)^2 = x^{(3)(2)} = x^6$			
7	$(xy)^n = x^n y^n$	$(xy)^3 = x^3y^3$			
8	$(\frac{x}{y})^n = \frac{x^n}{y^n}$	$(\frac{x}{y})^3 = \frac{x^3}{y^3}$			
9	$x^{-n} = \frac{1}{x^n}$	$x^{-2} = \frac{1}{x^2}$			
0			GEI		

Squares and Square Roots of Positive Rational Numbers

Recommendations for Test-Takers

- Memorize the first 12 perfect squares (1, 4, 9, ..., 144)
- Understand inverse relationships between pairs of squares and square roots ($12^2 = \sqrt{144}$ and $\sqrt{144} = 12$)
- Understand difference in squaring a negative number and the negative of a square number, i.e., $(-3)^2 = 9$ and $-(-3)^2 = -9$
- Practice computing with square and square roots that include fractions and decimals



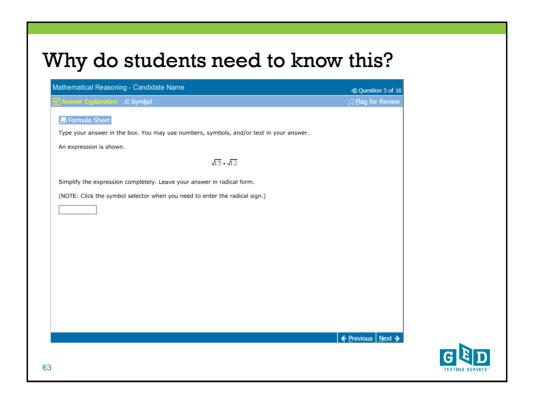
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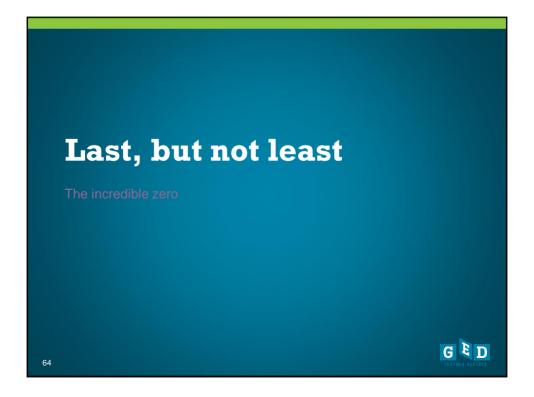
Simplifying Radical Expressions

- √9
- Find the prime factors = $\sqrt{3 \cdot 3}$
- Bring any pairs outside the radical = 3

$$\sqrt{9xy^2}
\sqrt{3 \cdot 3 \cdot x \cdot y \cdot y}
3y\sqrt{x}$$







The Incredible Zero

- It is unique in representing nothingness.
- As a placeholder it gives our number system its power.
- It acquires different meaning based on its location. Think 30 versus 3,000.



The Origin of the Number Zero

http://www.smithsonianmag.com/history/origin-number-zero-180953392/#qagAYijydW3RXhhk.99



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Properties of Zero

Property	Example
a + 0 = a	4 + 0 = 4
a – 0 = a	4 - 0 = 4
$a \times 0 = 0$	6 × 0 = 0
0 / a = 0	0/3 = 0
a / 0 = undefined (<u>dividing by zero is undefined</u>)	7/0 = undefined
0 ^a = 0 (a is positive)	0 ⁴ = 0

http://www.mathsisfun.com/numbers/zero.html



The Problem with Zero



 $\frac{7}{0}$

You can express a fraction with 0 in the denominator, but it has no meaning.

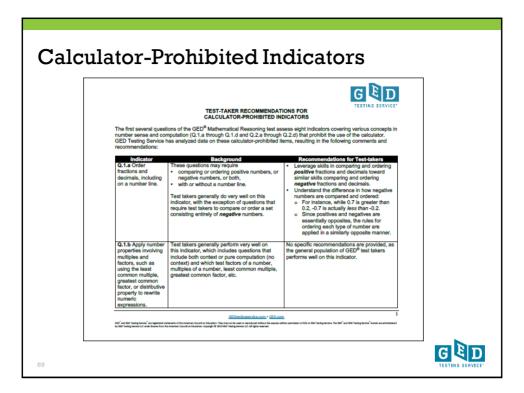
Division by zero is undefined. Mathematicians have never defined the meaning because there is no good definition. How many times can you throw nothing into no baskets?

As many times as you want. It's just not a real number.

To learn more: https://www.khanacademy.org/math/algebra/introduction-to-algebra/division-by-zero/v/why-dividing-by-zero-is-undefined







Sample Items Order Fractions and Decimals Place the following numbers in order from greatest to least: 0.2, -1/2, 0.6, 1/3, 1, 0, 1/6 Factors and Multiples Find the LCM that is necessary to perform the indicated operation. 7/6 – 1/4 = Rules of Exponents Simplify the following: (x³)5 Distance on a Number Line Find the distance between two points -9 and -3 on a number line

Sample Items

Operations on Rational

Solve: $3(\frac{1}{2}) \div 3\frac{1}{2} =$

Numbers

Squares and Square Roots of Find $\sqrt{9}$ Find $\sqrt{24}$

Positive Rational Numbers

Cubes and Cube Roots of

Find (-4)3

Rational Numbers

of Real Numbers

Undefined Value Over the Set Solve (2x - 3)(x + 2) = 0



Tips for Building Foundational Skills



- Help students build their number sense
- Include opportunities for students to work together
- Provide plenty of practice with real-life situations included
- Set high expectations





